

# A comparison of $K_{DP}$ retrieval algorithms in an idealized known-truth environment

\*Karly Jackson Reimel<sup>1</sup>, Matthew R Kumjian<sup>1</sup>

1. Pennsylvania State University

Specific differential phase ( $K_{DP}$ ) is a popular choice for polarimetric radar rainfall estimation and attenuation correction. Unfortunately,  $K_{DP}$  is not straightforward to retrieve because polarimetric radars do not directly measure  $K_{DP}$ . Instead, radars measure the total differential phase shift ( $\Psi_{DP}$ ), which comprises the accumulated differential phase shift owing to propagation ( $\Phi_{DP}$ ) and the backscatter differential phase shift ( $\delta$ ). To accurately estimate  $K_{DP}$ , one must remove  $\delta$  from the  $\Psi_{DP}$  profile to isolate  $\Phi_{DP}$ , and then take half the range derivative of  $\Phi_{DP}$ .  $\Phi_{DP}$  is inherently noisy owing to measurement errors, which can lead to uncertain  $K_{DP}$  estimates; therefore,  $\Phi_{DP}$  must be smoothed before taking its derivative. There are numerous published methods tackling this smoothing problem, each with varying complexity. For example, some simply fit a line to the  $\Phi_{DP}$  profile; others use more advanced methods (e.g., a Kalman filter) to smooth  $\Phi_{DP}$ . A few algorithms even use other radar variables, such as  $Z_H$ , to determine where sharp gradients in  $K_{DP}$  might be expected. Each proposed algorithm successfully smooths  $\Phi_{DP}$  and retrieves  $K_{DP}$ , but it is unclear which algorithms are most accurate and what the resulting  $K_{DP}$  estimate uncertainty is. To address this problem, we analyze and compare seven  $K_{DP}$  estimation algorithms using an idealized framework. We create a synthetic ( “true” )  $K_{DP}$  profile, and then integrate over it to obtain the “smoothed”  $\Phi_{DP}$ . We then add noise typical of weather radar measurements and apply each algorithm to our noisy  $\Phi_{DP}$  profile. The algorithm-estimated  $K_{DP}$  profiles are compared to our known truth profile, and the errors and uncertainty are quantified. The synthetic  $K_{DP}$  profiles are Gaussian in shape, allowing us to vary their magnitude and width to determine how each algorithm performs in smooth, slowly changing  $K_{DP}$  profiles, as well as steep and peaked profiles. We show that the algorithm errors vary over the range of different Gaussian widths and peak values. The overall patterns of these errors also change between algorithms, suggesting that the performance of each algorithm is dependent on the type of  $\Phi_{DP}$  profile it receives. This result is further supported by an error analysis of each algorithm for a set of more complicated synthetic  $K_{DP}$  profiles.

Keywords: specific differential phase, KDP, retrieval, uncertainty